

Vector Interpretations

Basic directional vectors are always of the form $\langle \text{horizontal change}, \text{vertical change} \rangle$, or $\langle x \text{ component}, y \text{ component} \rangle$. Keep in mind east is in the x direction, west is the $-x$ direction, north is in the y direction and south is the $-y$ direction.

Examples of moving 5 miles in each direction:

Direction	Graph	Vector Set-up
East 5 \rightarrow		$\langle 5, 0 \rangle$
West 5 \rightarrow		$\langle -5, 0 \rangle$
North 5 \rightarrow		$\langle 0, 5 \rangle$
South 5 \rightarrow		$\langle 0, -5 \rangle$
Northeast 5 \rightarrow		$\langle 5\cos(45^\circ), 5\sin(45^\circ) \rangle$
Northwest 5 \rightarrow		$\langle 5\cos(135^\circ), 5\sin(135^\circ) \rangle$
Southeast 5 \rightarrow		$\langle 5\cos(315^\circ), 5\sin(315^\circ) \rangle$
Southwest 5 \rightarrow		$\langle 5\cos(225^\circ), 5\sin(225^\circ) \rangle$

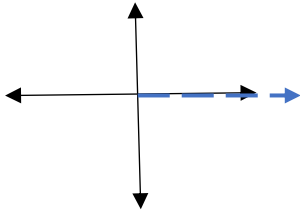
Example:

You start at home and take a morning walk. You follow the path of:

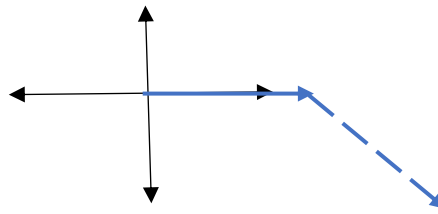
- 5 miles east
- 10 miles southeast
- 3 miles south
- 2 miles southwest

Let's draw the picture and break each step into components.

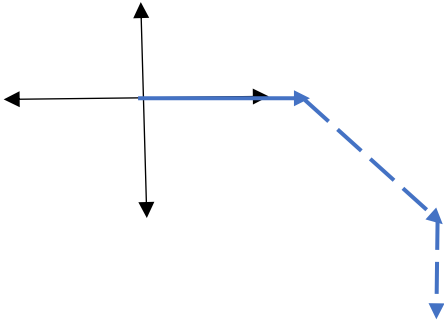
5 miles east



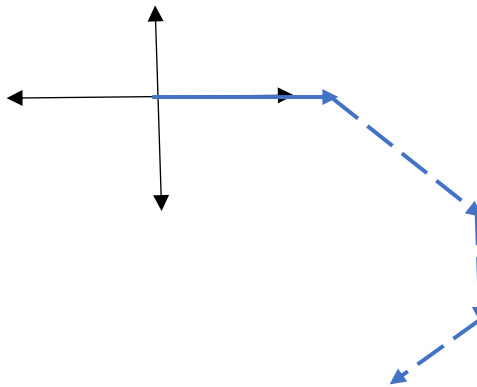
10 miles southeast



3 miles south



2 miles southwest



a) How far did you walk: $5 + 10 + 3 + 2 = 20$ miles

	Horizontal component(x)	Vertical component(y)
5 miles east	5	0
10 miles southeast	$10\cos(315^\circ)$	$10\sin(315^\circ)$
3 miles south	0	-3
2 miles southwest	$2\cos(225^\circ)$	$2\sin(225^\circ)$
Resultant(sum)	10.657	-11.485

b) Displacement vector: $\langle 10.657, -11.485 \rangle$

c) Magnitude: $\sqrt{(10.657)^2 + (-11.485)^2} = 15.67$ miles from home if you walk back on a straight line